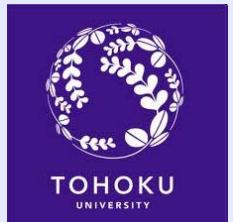
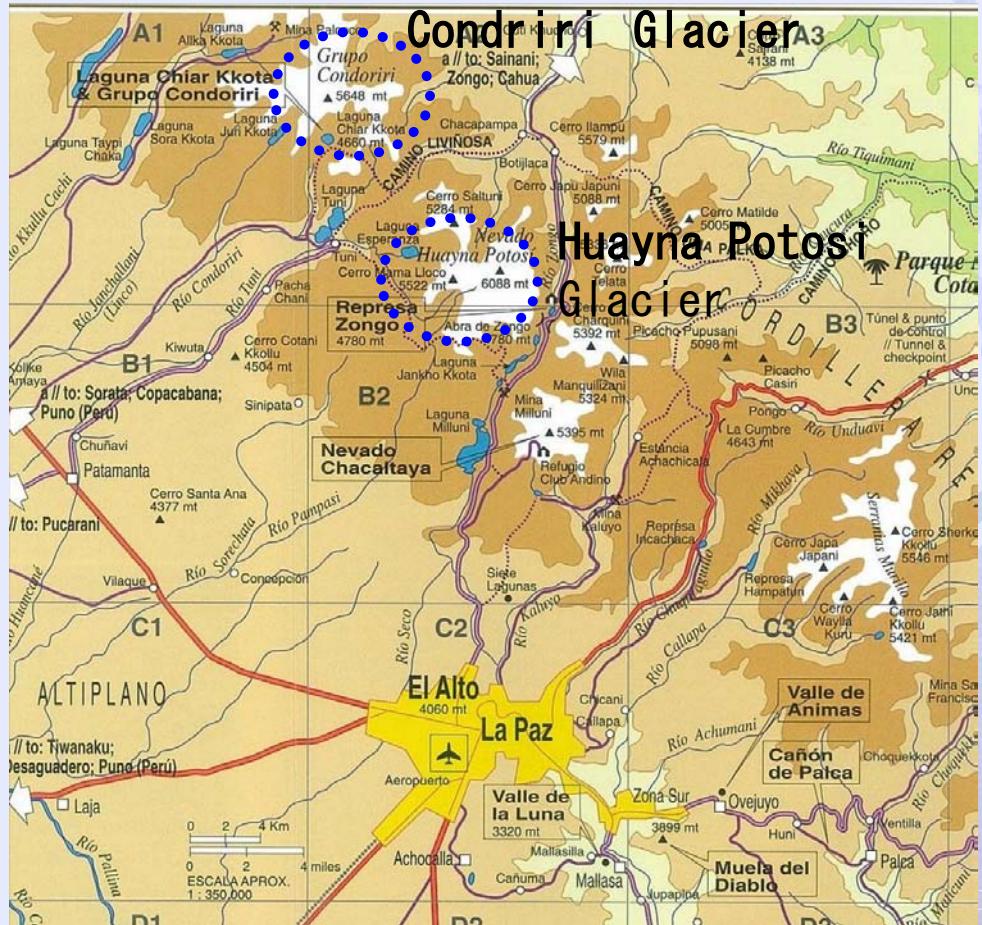


# Numerical simulation of 2D flow and sediment transport at a river entrance



Prof. Hitoshi TANAKA  
TOHOKU University

# 1. Introduction



# Research Framework



Group1  
Snow  
and Ice

Group2  
Ruff  
noff

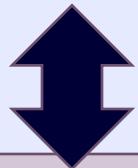
Group3  
Sediment

Group4  
Water  
Quality

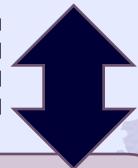
Group5  
Management



Instituto de Hidraulica e Hidrologia (IHH)  
Universidad Mayor de San Andres (UMSA)



MC & Ph.D. students, researchers

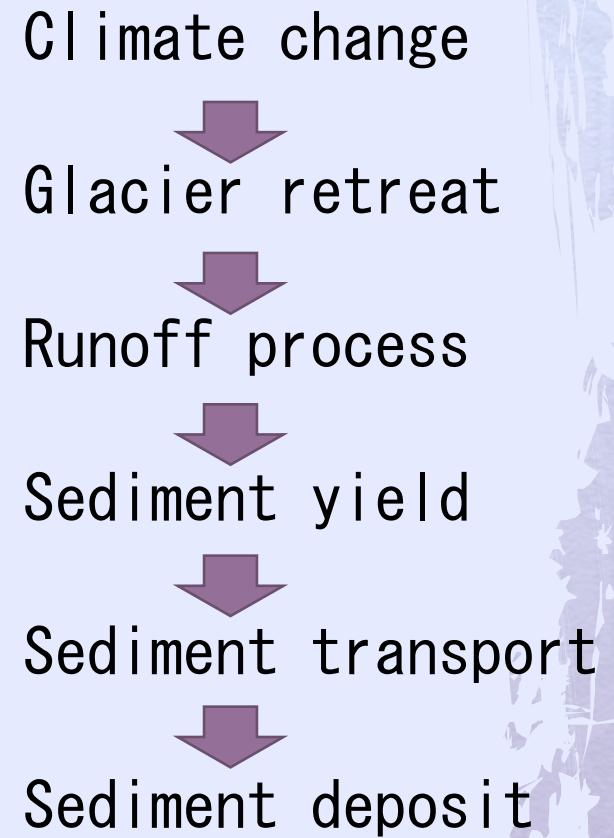


Tohoku University (TU)

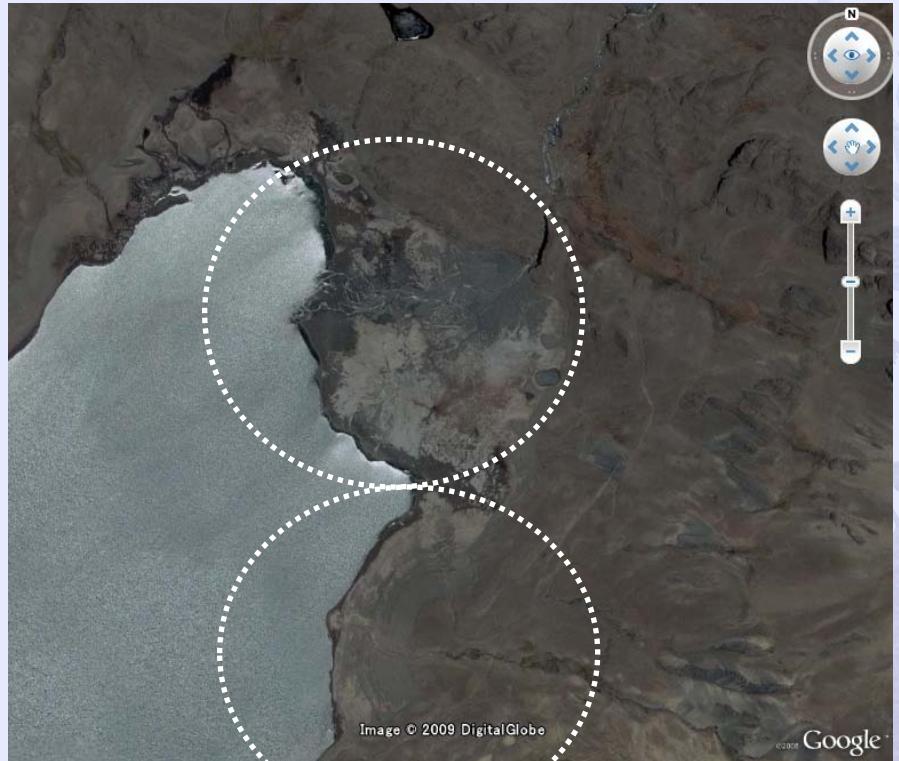
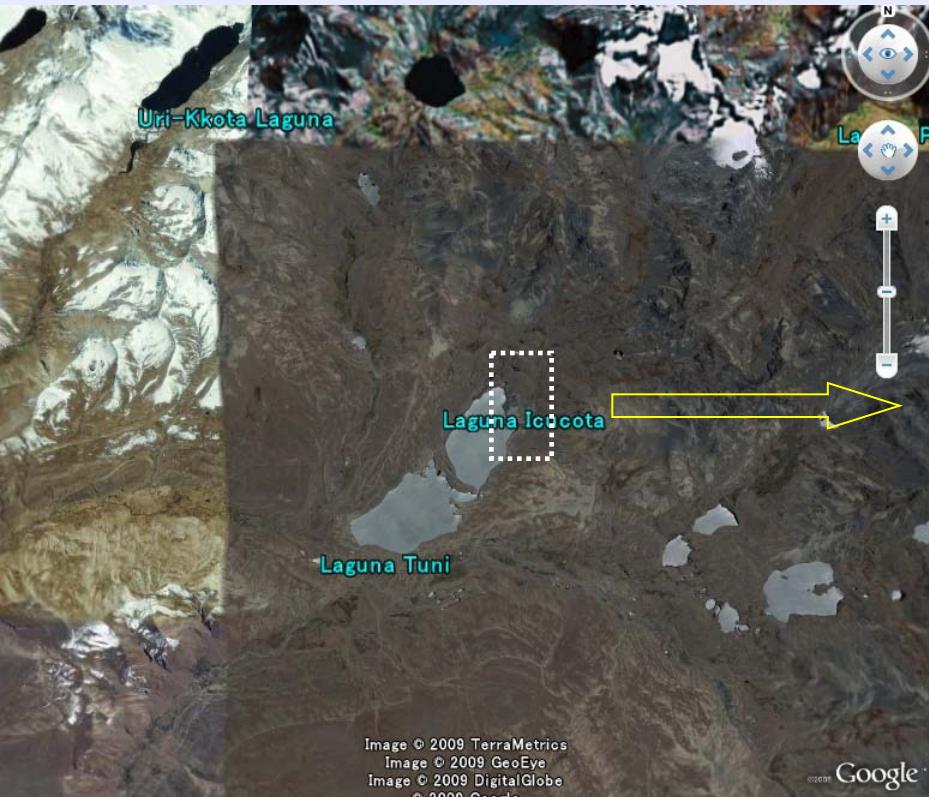
Tokyo Institute  
of Technology

Fukushima  
University

# SEDIMENTATION STUDY



# Sediment deposit in Lake Tuni(1)



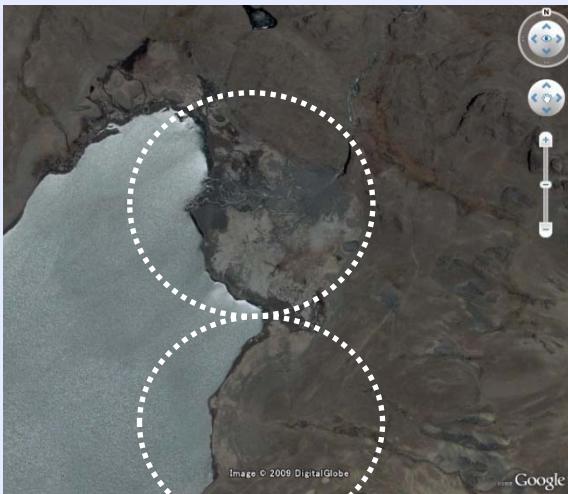
Objective:

Mathematical modeling of fluvial fan development  
in a reservoir - its modification due to climate  
change-

# Sediment deposit in Lake Tuni(2)



Sediment deposit in Lake Tuni (1)



Tuni River  
←



Sediment deposit in Lake Tuni (2)

# Sediment deposit in a glacier lake

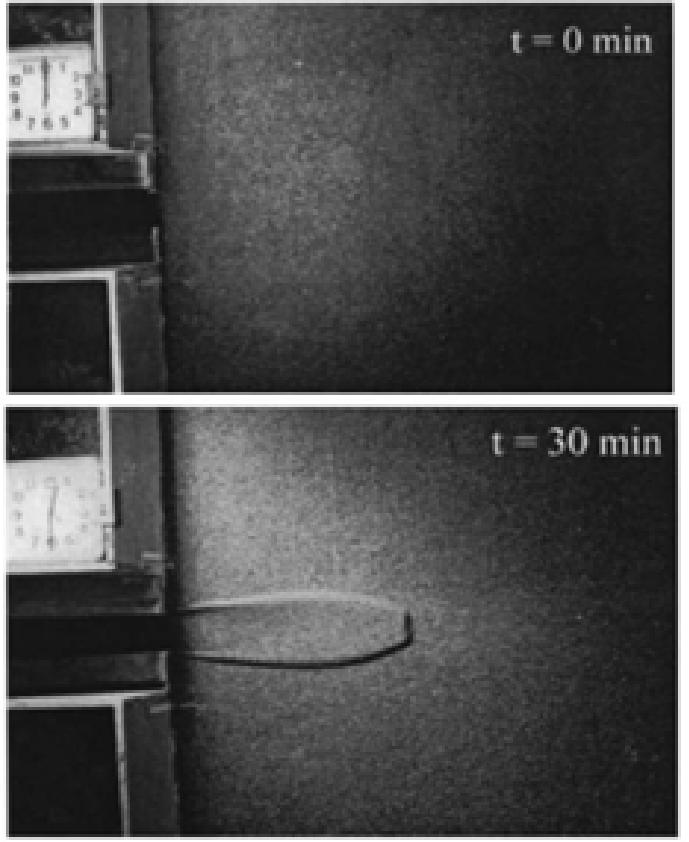
Huayna Potosí  
Glacier, Sep.  
2010



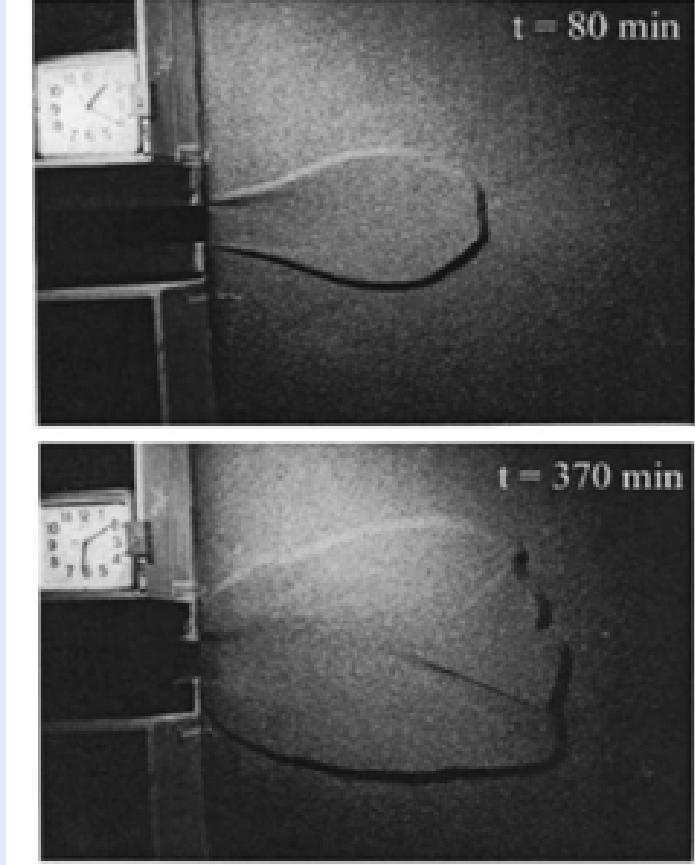
Sediment deposit  
in a glacier  
lake



# Sand terrace development in a lake (1)



(1)



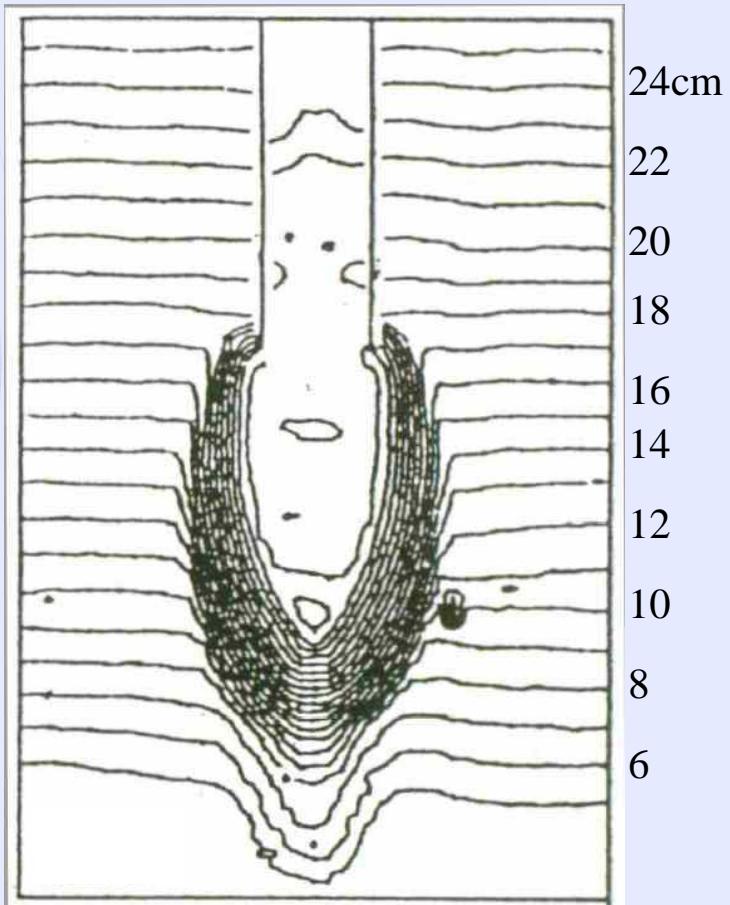
(2)

(3)

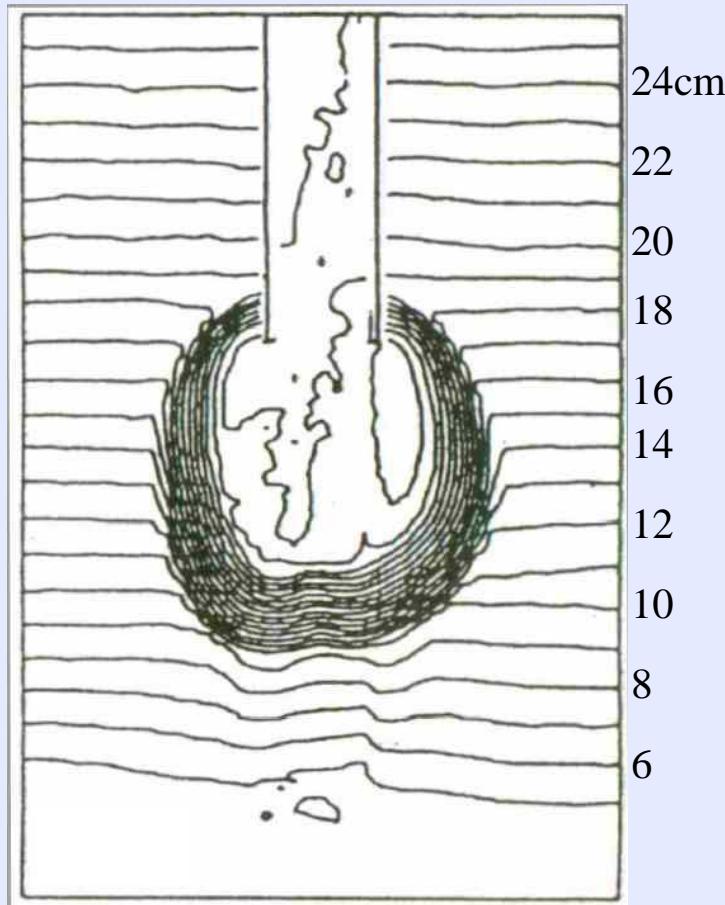
(4)

(Tseng et al., 2007)

# Sand terrace development in a lake (2)



(a) Case J



(b) Case K

(Tanaka, 2010)

## 2. Numerical simulation method

- ◆ Conservation equations for mass and momentum

$$\frac{\partial \eta}{\partial t} + \frac{\partial M}{\partial x} + \frac{\partial N}{\partial y} = 0$$

$$\frac{\partial M}{\partial t} + \frac{\partial}{\partial x} \left( \frac{M^2}{D} \right) + \frac{\partial}{\partial y} \left( \frac{MN}{D} \right) + gD \frac{\partial \eta}{\partial x} + \frac{\tau_x}{\rho} = 0$$

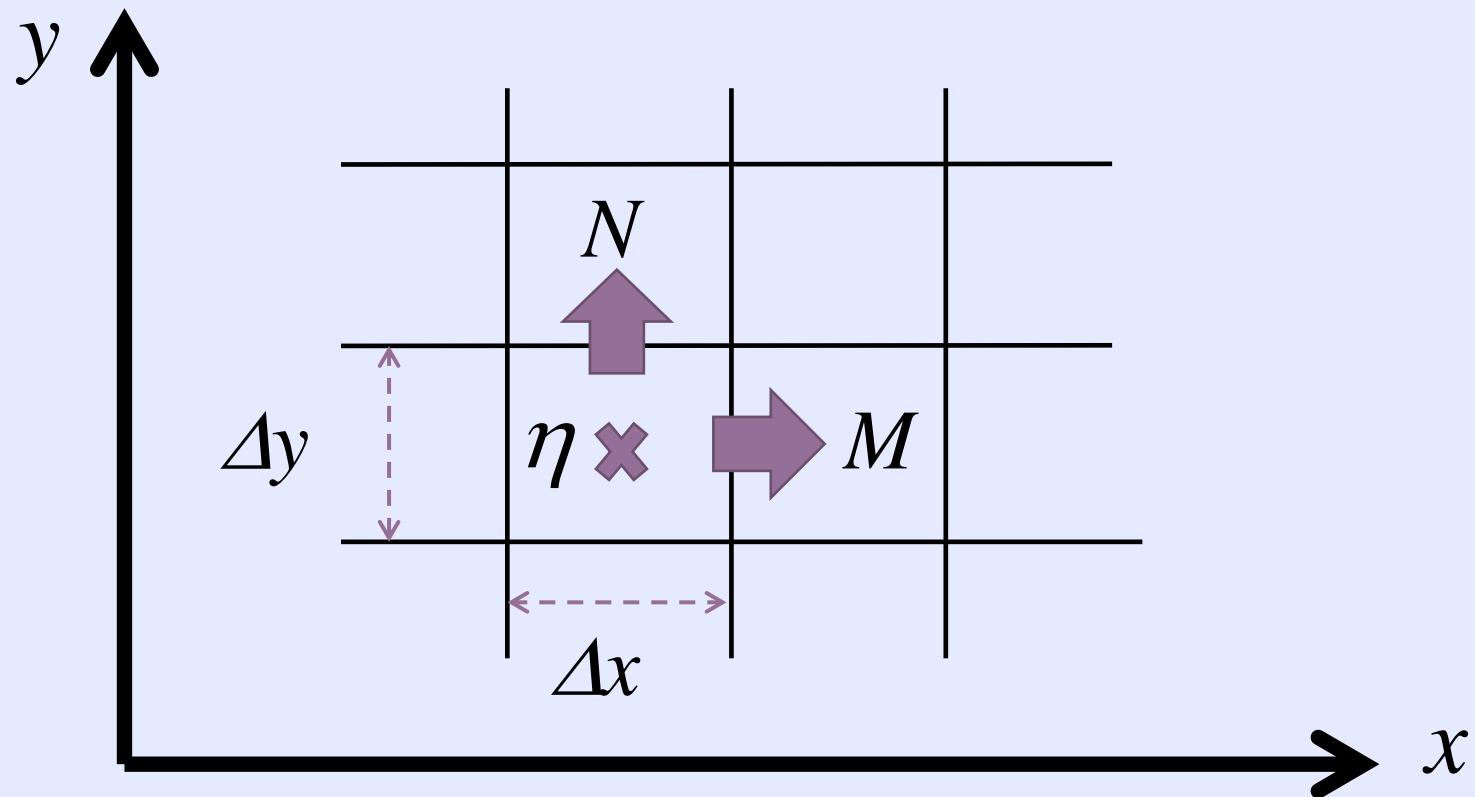
$$\frac{\partial N}{\partial t} + \frac{\partial}{\partial x} \left( \frac{MN}{D} \right) + \frac{\partial}{\partial y} \left( \frac{N^2}{D} \right) + gD \frac{\partial \eta}{\partial y} + \frac{\tau_y}{\rho} = 0$$

$\eta$  : the water level above the still water elevation,  $t$  : the time,  $x$  and  $y$  the horizontal coordinates,  $M$  and  $N$  the flow flux per unit width in  $x$ - and  $y$ -direction, respectively,  $g$  the gravitational acceleration,  $D$  the total water depth ( $D=h+\eta$ ,  $h$ : still water depth), and  $n$  is Manning's friction coefficient. Using  $M$ ,  $N$  and  $\eta$

◆ Bottom shear stress

$$\frac{\tau_x}{\rho} = \frac{gn^2}{D^{7/3}} M \sqrt{M^2 + N^2}$$

$$\frac{\tau_y}{\rho} = \frac{gn^2}{D^{7/3}} N \sqrt{M^2 + N^2}$$



## ◆ Sediment transport rate

Meyer-Peter-Muller formula with bed slope correction

$$q_B^* = 8(\tau^* - \tau_{cr}^*)^{1.5}$$

$$q_{BI}^* = q_B^*/C_I$$

$$C_I = \cos \theta \left( 1 - \frac{\sigma}{\sigma - \rho} \frac{\tan \theta}{\mu_s} \right)$$

$\theta$  :bed slope,  $\sigma$  :density of sand particle,  
 $\mu_s$  :coefficient of static friction

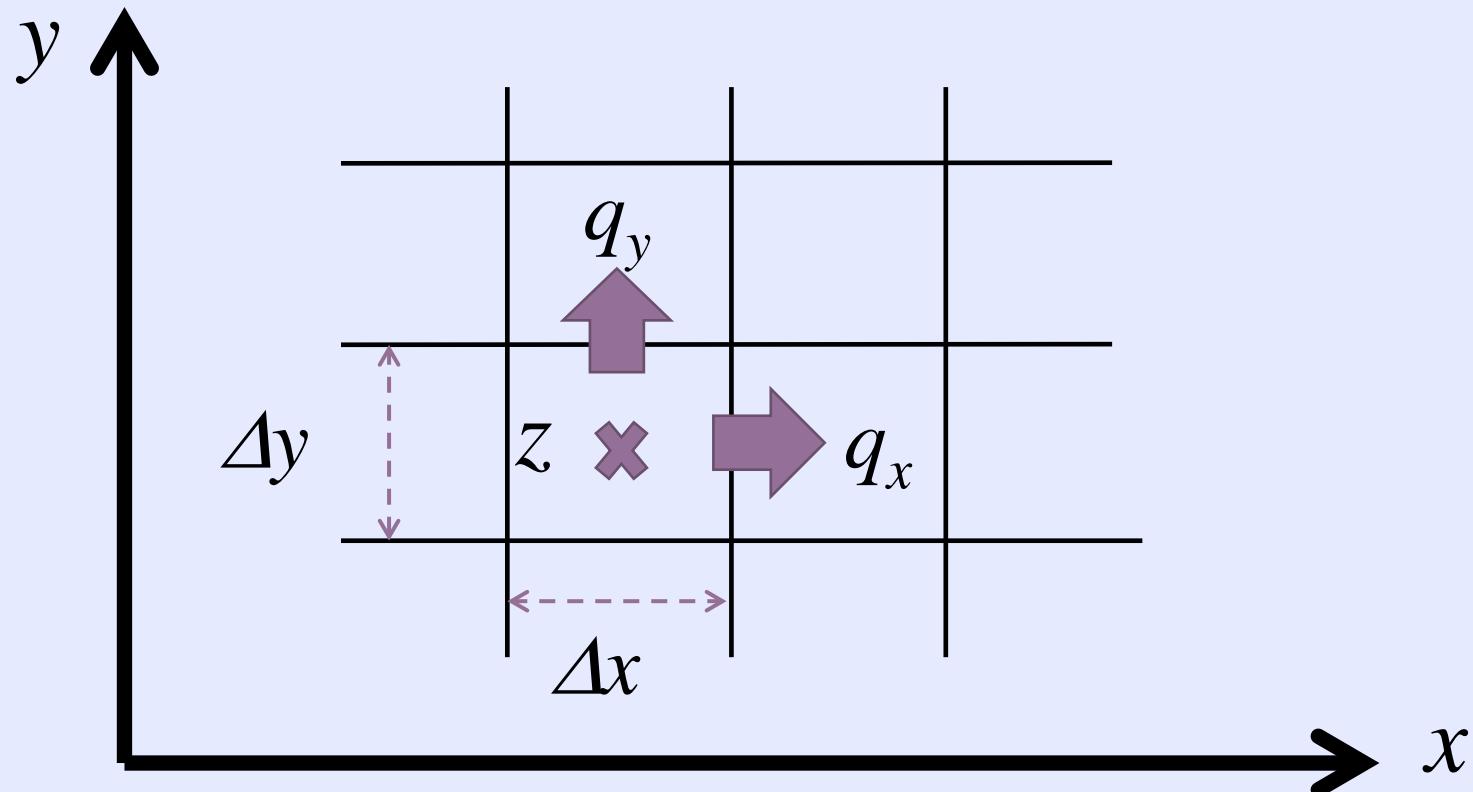
## ◆ Conservation of sediment mass

$$\frac{\partial z}{\partial t} + \frac{1}{1-\lambda} \left( \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} \right) = 0$$

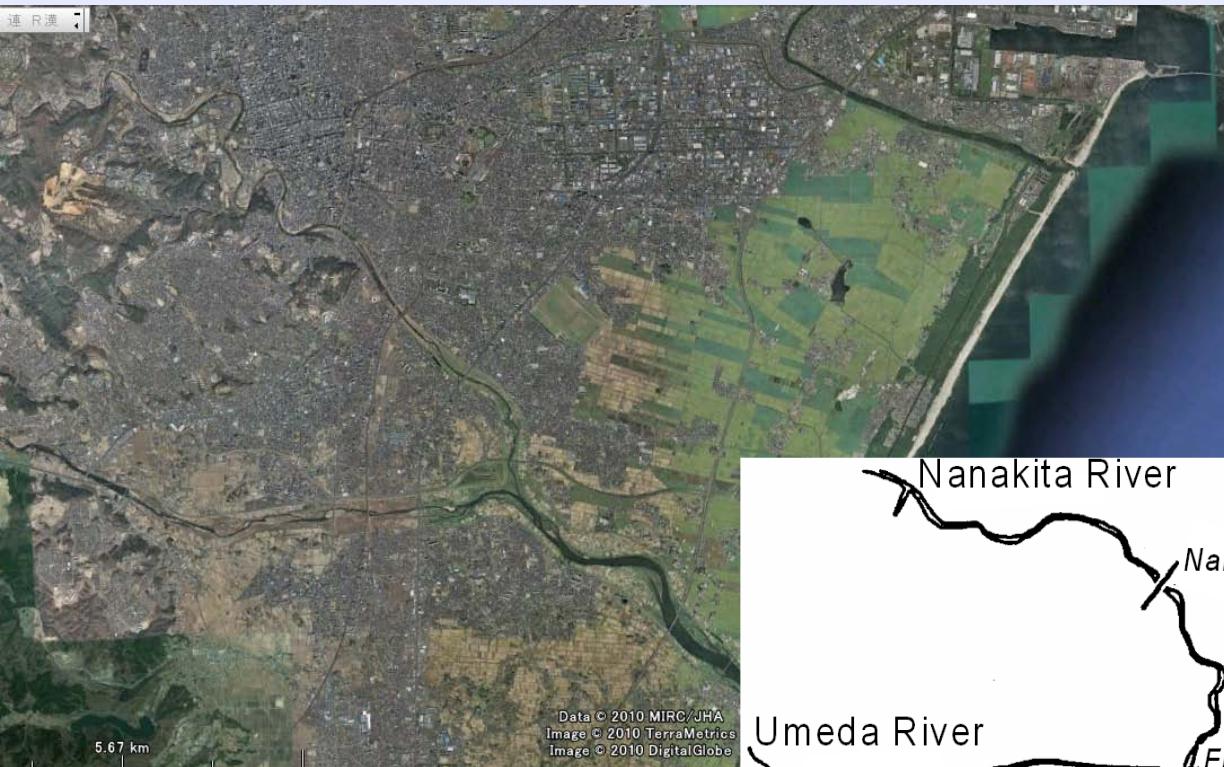
# ◆ Computation of river bed evolution



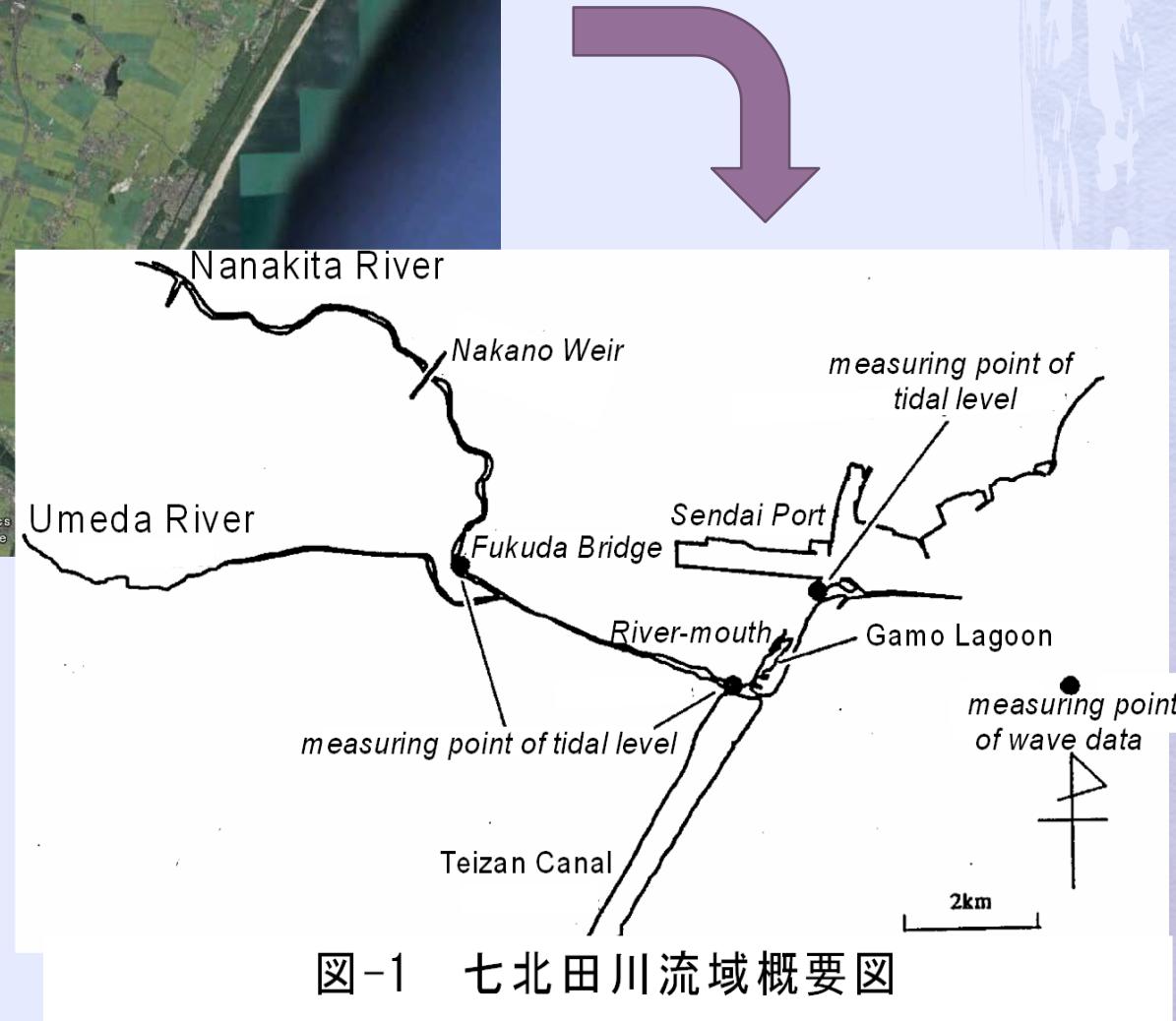
$$\frac{\partial z}{\partial t} + \frac{1}{1-\lambda} \left( \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} \right) = 0$$



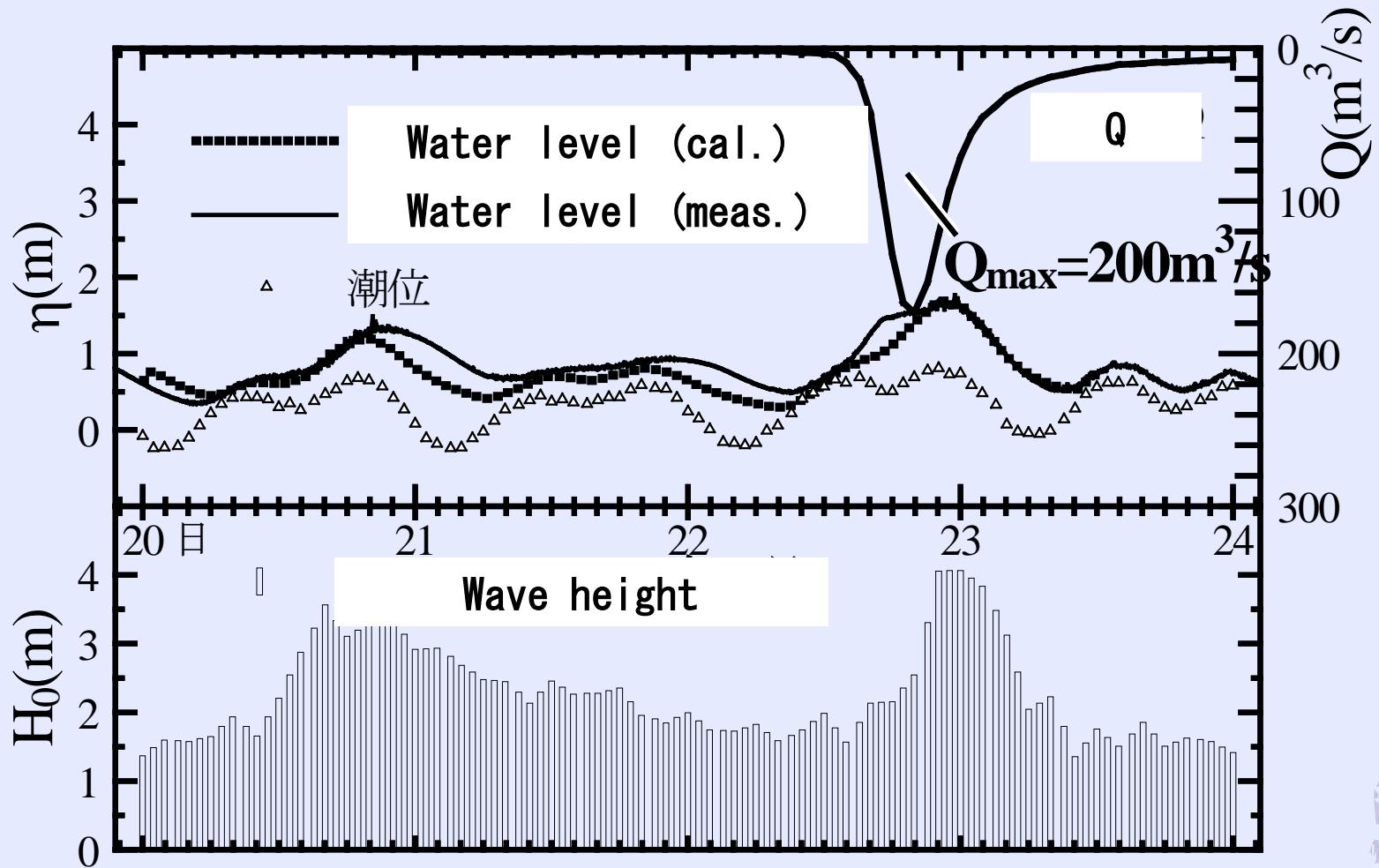
### 3. Computation results



#### Nanakita River

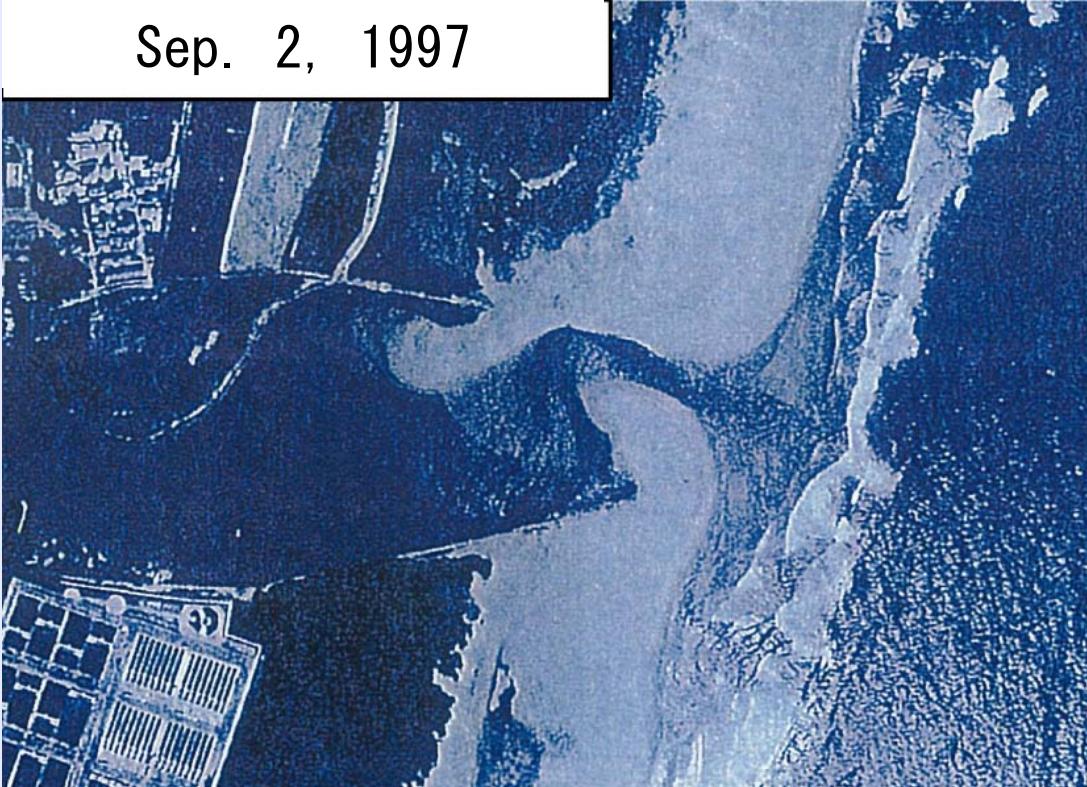


# Calibration against 1996 flood event

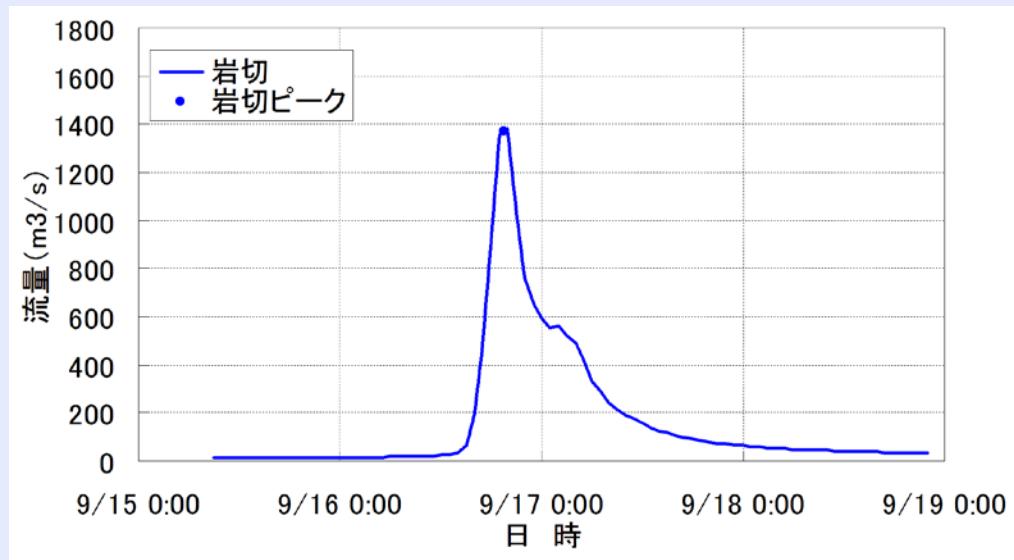


# Initial condition

Sep. 2, 1997

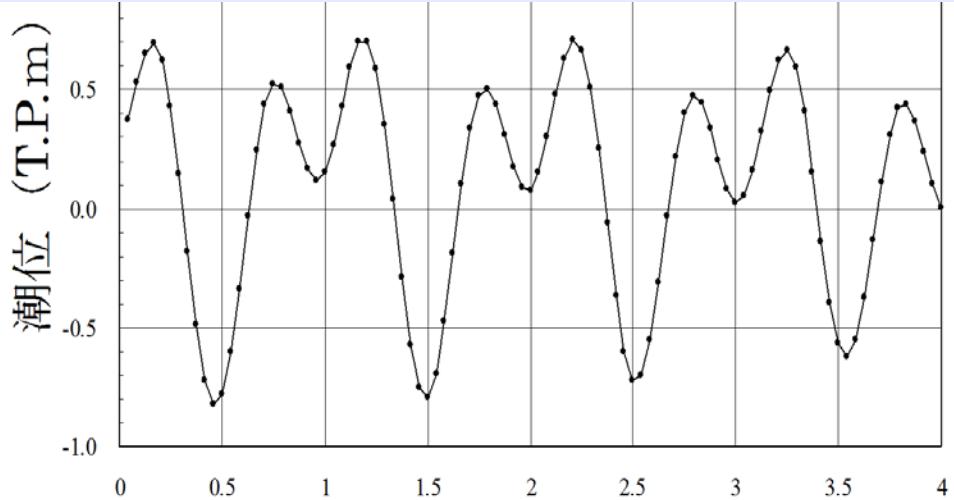


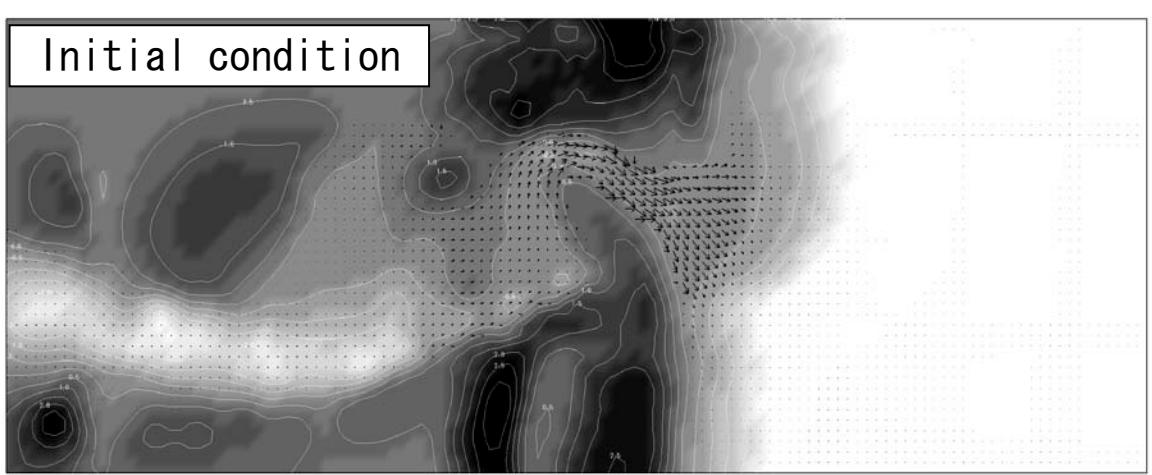
# Computation for a design flood



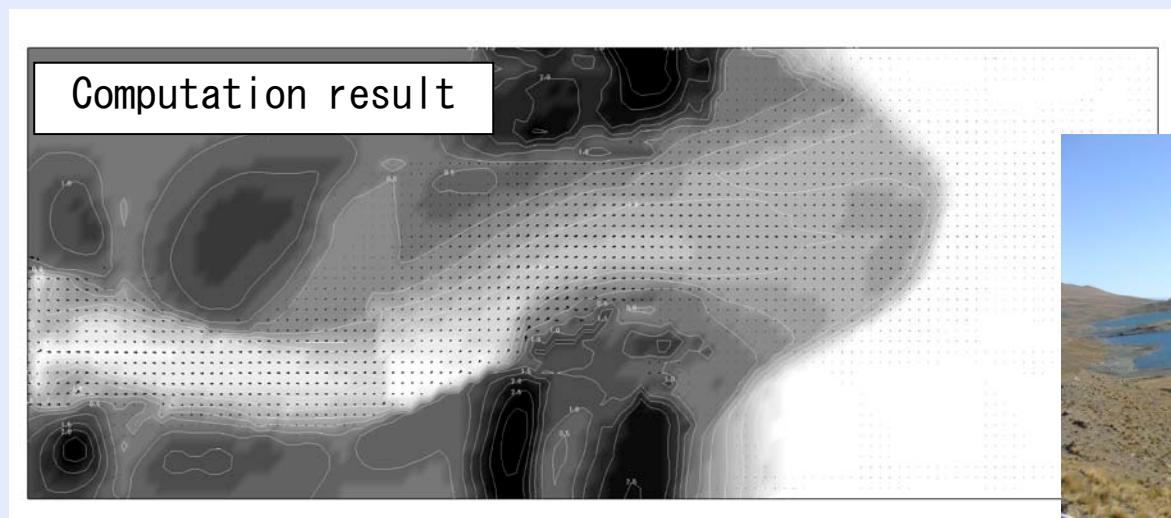
discharge ( $\text{m}^3/\text{s}$ )

tidal variation





3m





# Thank you for your kind attention!

## Gracias!







2004. 10. 25

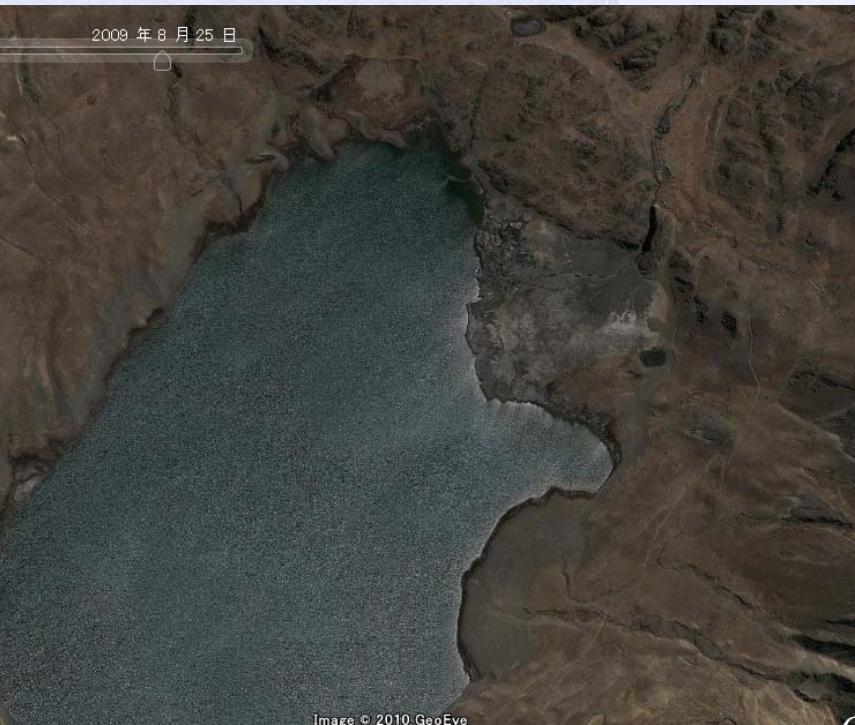


Image © 2010 GeoEye